## Pearson Edexcel

Mark Scheme (Results)

Summer 2019

Pearson Edexcel GCE Further Mathematics AS Further Statistics 1 Paper 8FM0_23

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## General Marking Guidance

- All candidates must receive the same treatment. Examiners must mark the first candidate in exactly the same way as they mark the last.
- Mark schemes should be applied positively. Candidates must be rewarded for what they have shown they can do rather than penalised for omissions.
- Examiners should mark according to the mark scheme not according to their perception of where the grade boundaries may lie.
- There is no ceiling on achievement. All marks on the mark scheme should be used appropriately.
- All the marks on the mark scheme are designed to be awarded. Examiners should always award full marks if deserved, i.e. if the answer matches the mark scheme. Examiners should also be prepared to award zero marks if the candidate's response is not worthy of credit according to the mark scheme.
- Where some judgement is required, mark schemes will provide the principles by which marks will be awarded and exemplification may be limited.
- When examiners are in doubt regarding the application of the mark scheme to a candidate's response, the team leader must be consulted.
- Crossed out work should be marked UNLESS the candidate has replaced it with an alternative response.


## EDEXCEL GCE MATHEMATICS

## General Instructions for Marking

1. The total number of marks for the paper is 40 .
2. The Edexcel Mathematics mark schemes use the following types of marks:

- M marks: method marks are awarded for 'knowing a method and attempting to apply it', unless otherwise indicated.
- A marks: Accuracy marks can only be awarded if the relevant method (M) marks have been earned.
- B marks are unconditional accuracy marks (independent of M marks)
- Marks should not be subdivided.

3. Abbreviations

These are some of the traditional marking abbreviations that will appear in the mark schemes.

- bod - benefit of doubt
- ft - follow through
- the symbol $\sqrt{ }$ will be used for correct ft
- cao - correct answer only
- cso - correct solution only. There must be no errors in this part of the question to obtain this mark
- isw - ignore subsequent working
- awrt - answers which round to
- SC: special case
- oe - or equivalent (and appropriate)
- dep - dependent
- indep - independent
- dp decimal places
- sf significant figures
-     * The answer is printed on the paper
- $\square$ The second mark is dependent on gaining the first mark

4. For misreading which does not alter the character of a question or materially simplify it, deduct two from any A or B marks gained, in that part of the question affected.
5. Where a candidate has made multiple responses and indicates which response they wish to submit, examiners should mark this response.
If there are several attempts at a question which have not been crossed out, examiners should mark the final answer which is the answer that is the most complete.
6. Ignore wrong working or incorrect statements following a correct answer.
7. Mark schemes will firstly show the solution judged to be the most common response expected from candidates. Where appropriate, alternatives answers are provided in the notes. If examiners are not sure if an answer is acceptable, they will check the mark scheme to see if an alternative answer is given for the method used.

| Qu | Scheme | Marks | AO |
| :---: | :---: | :---: | :---: |
| 1(a) | $\mathrm{H}_{0}$ : There is no association between age and activity <br> $\mathrm{H}_{1}$ : There is an association between age and activity | B1 | 1.2 |
| (b) | $\frac{26 \times 36}{150}=6.24$ | (1) | 1.1b |
|  | Since expected value in $a<20$ and snooker $=3.6<5$ | (1) | 2.4 |
| (c) | we amalgamate two rows <br> Table is now $4 \times 3$ so degrees of freedom is ( $4-1) \times(3-1)=6(*)$ | $\begin{aligned} & \mathrm{B} 1 \\ & \mathrm{~B} 1^{*} \end{aligned}$ | 1.1b |
| (d) | Critical value $\chi_{6}{ }^{2}(5 \%)=12.592$ | B1 | 1.1b |
|  | [Significant result]: so there is evidence to support manager's belief | B1ft <br> (2) <br> marks) | 2.2b |
| Notes |  |  |  |
| (a) B1 for both hypotheses in terms of "association" or "independence". Must mention age and activity (or sport). [Use of "relationship" or "link" here is B0 but allow for last B1ft] |  |  |  |
| (b) | B1 for 6.24 |  |  |
| (c) | $2^{\text {nd }} B 1$ * for 6 degrees of freedom clearly coming from a $4 \times 3$ table formed from amalgamation of rows. [ $8-2=6$ is B 0 ] |  |  |
| (d) | $1^{\text {st }} \mathrm{B} 1$ for correct critical value (allow 12.6 or 12.59 or awrt 12.592) NB $p$-value $=0.0032839 \ldots$ so allow awrt 0.00328 <br> $2^{\text {nd }} \mathrm{B} 1 \mathrm{ft}$ for a correct comparison and conclusion (ft their cv) [Independent of hypotheses] e.g. there is an "association" or "relationship" or "link" between age and activity is OK <br> BUT there is a "correlation" between age and activity is B0 <br> Do not accept contradictory contextual statements e.g. "manager's belief supported , there is no association between age and activity" |  |  |

\begin{tabular}{|c|c|c|c|c|c|c|c|c|}
\hline Qu \& \multicolumn{6}{|c|}{Scheme} \& Marks \& AO \\
\hline \multirow[t]{6}{*}{2.} \& \multicolumn{6}{|l|}{\begin{tabular}{l}
\(\mathrm{H}_{0}\) : Spinner is working as designed (o.e.) \\
\(\mathrm{H}_{1}\) : Spinner is not working as designed (o.e.)
\end{tabular}} \& B1 \& 1.2 \\
\hline \& \(E_{i}\) \& 24 \& 8 \& 8 \& 32 \& 8 \& \multirow[t]{2}{*}{M1
A1} \& \multirow[t]{2}{*}{\[
\begin{aligned}
\& 3.4 \\
\& 1.1 \mathrm{~b}
\end{aligned}
\]} \\
\hline \& \(O_{i}\) \& 15 \& 4 \& 12 \& 41 \& 8 \& \& \\
\hline \& \(\frac{\left(O_{i}-E_{i}\right)^{2}}{E_{i}}\) \& \(\frac{81}{24}\) \& \(\frac{16}{8}\) \& \(\frac{16}{8}\) \& \(\frac{81}{32}\) \&  \& \multirow[t]{2}{*}{M1} \& 1.1b \\
\hline \& \(\frac{O_{i}{ }^{2}}{E_{i}}\) \& \[
\frac{225}{24}
\] \& \[
\frac{16}{8}
\] \& \[
\frac{144}{8}
\] \& \[
\frac{1681}{32}
\] \& \[
\frac{64}{8}
\] \& \& \\
\hline \& \multicolumn{6}{|l|}{\begin{tabular}{l}
\[
\begin{aligned}
\& \sum \frac{\left(O_{i}-E_{i}\right)^{2}}{E_{i}}=3.375+2+2+2.53125+0=9.90625 \\
\& \text { or } \sum \frac{O_{i}^{2}}{E_{i}}-N=9.375+2+18+52.53125+8-80=9.90625 \\
\& v=5-1=4 \quad \text { so } \quad \chi_{4}^{2}(10 \%) \mathrm{cv}=7.779 \text { or better }
\end{aligned}
\] \\
Result is significant so there is evidence that the spinner is not operating as designed
\end{tabular}} \& \begin{tabular}{l}
A1 \\
B1 \\
A1cso \\
marks)
\end{tabular} \& 1.1 b

3.4
3.5 a <br>
\hline \multicolumn{9}{|c|}{Notes} <br>

\hline | $1^{\text {st }} \mathrm{B} 1$ for both hypotheses given in suitable context |
| :--- |
| $1^{\text {st }}$ M1 for using the model to find at least 2 correct expected frequencies |
| $1^{\text {st }}$ A1 for all correct $E_{i}$ |
| $2^{\text {nd }}$ M1 for attempt to find test statistic (at least two correct expressions, fractions or decimals) |
| $2^{\text {nd }} \mathrm{A} 1$ for a correct test statistic (awrt 9.91) [ accept $\frac{317}{32}$ ] |
| $2^{\text {nd }} \mathrm{B} 1$ for correct critical value (allow 7.78) |
| NB $p$ - value $=0.042036 \ldots$ so allow awrt 0.042 |
| $3^{\text {rd }}$ A1cso dep on all previous marks for a correct conclusion in context |
| (can be in terms of model or spinner's design) Must mention spinner and scores or design Accept "spinner is not accurate" | \& \multicolumn{8}{|l|}{| $1^{\text {st }} \mathrm{B} 1$ for both hypotheses given in suitable context |
| :--- |
| $1^{\text {st }} \mathrm{M} 1$ for using the model to find at least 2 correct expected frequencies |
| $1^{\text {st }}$ A1 for all correct $E_{i}$ |
| $2^{\text {nd }}$ M1 for attempt to find test statistic (at least two correct expressions, fractions or decimals) |
| $2^{\text {nd }}$ A1 for a correct test statistic (awrt 9.91) [ accept $\frac{317}{32}$ ] |
| $2^{\text {nd }} \mathrm{B} 1$ for correct critical value (allow 7.78) |
| NB $p$-value $=0.042036 \ldots$ so allow awrt 0.042 |
| $3^{\text {rd }}$ A1cso dep on all previous marks for a correct conclusion in context (can be in terms of model or spinner's design) Must mention spinner and scores or design Accept "spinner is not accurate" |} <br>

\hline
\end{tabular}




