## Pearson Edexcel

# Mark Scheme (Results) 

Summer 2022

Pearson Edexcel GCE
In Further Mathematics (8FM0)
Paper 25 Further Mechanics 1

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- All candidates must receive the same treatment. Examiners must mark the first candidate in exactly the same way as they mark the last.
- Mark schemes should be applied positively. Candidates must be rewarded for what they have shown they can do rather than penalised for omissions.
- Examiners should mark according to the mark scheme not according to their perception of where the grade boundaries may lie.
- There is no ceiling on achievement. All marks on the mark scheme should be used appropriately.
- All the marks on the mark scheme are designed to be awarded. Examiners should always award full marks if deserved, i.e. if the answer matches the mark scheme. Examiners should also be prepared to award zero marks if the candidate's response is not worthy of credit according to the mark scheme.
- Where some judgement is required, mark schemes will provide the principles by which marks will be awarded and exemplification may be limited.
- When examiners are in doubt regarding the application of the mark scheme to a candidate's response, the team leader must be consulted.
- Crossed out work should be marked UNLESS the candidate has replaced it with an alternative response.


## EDEXCEL GCE MATHEMATICS General Instructions for Marking

1. The total number of marks for the paper is 40 .
2. The Edexcel Mathematics mark schemes use the following types of marks:

- M marks: method marks are awarded for 'knowing a method and attempting to apply it', unless otherwise indicated.
- A marks: Accuracy marks can only be awarded if the relevant method (M) marks have been earned.
- B marks are unconditional accuracy marks (independent of M marks)
- Marks should not be subdivided.

3. Abbreviations

These are some of the traditional marking abbreviations that will appear in the mark schemes.

- bod - benefit of doubt
- ft - follow through
- the symbol $\sqrt{ }$ will be used for correct ft
- cao - correct answer only
- cso - correct solution only. There must be no errors in this part of the question to obtain this mark
- isw - ignore subsequent working
- awrt - answers which round to
- SC: special case
- oe - or equivalent (and appropriate)
- dep - dependent
- indep - independent
- dp decimal places
- sf significant figures
-     * The answer is printed on the paper
- $\square$ The second mark is dependent on gaining the first mark

4. For misreading which does not alter the character of a question or materially simplify it, deduct two from any A or B marks gained, in that part of the question affected.
5. Where a candidate has made multiple responses and indicates which response they wish to submit, examiners should mark this response. If there are several attempts at a question which have not been crossed out, examiners should mark the final answer which is the answer that is the most complete.
6. Ignore wrong working or incorrect statements following a correct answer.
7. Mark schemes will firstly show the solution judged to be the most common response expected from candidates. Where appropriate, alternatives answers are provided in the notes. If examiners are not sure if an answer is acceptable, they will check the mark scheme to see if an alternative answer is given for the method used.

- Rules for M marks: correct no. of terms; dimensionally correct; all terms that need resolving (i.e. multiplied by cos or $\sin$ ) are resolved.
- Omission or extra g in a resolution is an accuracy error not method error.
- Omission of mass from a resolution is a method error.
- Omission of a length from a moments equation is a method error.
- Omission of units or incorrect units is not (usually) counted as an accuracy error.
- $d M$ indicates a dependent method mark i.e. one that can only be awarded if a previous specified method mark has been awarded.
- Any numerical answer which comes from use of $g=9.8$ should be given to 2 or 3 SF .
- Use of $g=9.81$ should be penalised once per (complete) question.
N.B. Over-accuracy or under-accuracy of correct answers should only be penalised once per complete question. However, premature approximation should be penalised every time it occurs.
- Marks must be entered in the same order as they appear on the mark scheme.
- In all cases, if the candidate clearly labels their working under a particular part of a question i.e. (a) or (b) or (c),......then that working can only score marks for that part of the question.
- Accept column vectors in all cases.
- Misreads - if a misread does not alter the character of a question or materially simplify it, deduct two from any A or B marks gained, bearing in mind that after a misread, the subsequent A marks affected are treated as A ft
- Mechanics Abbreviations

M(A) Taking moments about A
N2L Newton's Second Law (Equation of Motion)
NEL Newton's Experimental Law (Newton's Law of Impact)
HL Hooke's Law
SHM Simple harmonic motion
PCLM Principle of conservation of linear momentum
RHS, LHS Right hand side, left hand side

| Question |  | Scheme | Marks | AOs |
| :---: | :---: | :---: | :---: | :---: |
| 1. |  | $F=\frac{32000}{20}$ | M1 | 3.3 |
|  |  | Equation of motion | M1 | 3.1b |
|  |  | $F-1200 \mathrm{~g} \sin \alpha-R=1200 \times 0.5$ | A1 | 1.1b |
|  |  | Substitute for $g$, trig and $F$ and solve for $R$ | DM1 | 1.1b |
|  |  | $R=216$ or 220 ( N ) | A1 | 1.1b |
|  |  |  | (5) |  |
| (5 marks) |  |  |  |  |
| Notes: |  |  |  |  |
| 1 | M1 | Use of $P=F v$. Allow $\frac{32}{20}$. <br> Allow $32000=20 \mathrm{~F}$ or $32=20 \mathrm{~F}$, followed by an error when dividing M0 for $32000=20(F-R)$ or similar |  |  |
|  | M1 | Correct no. of terms, condone sign errors and sin/cos confusion M0 if they use power in equation of motion |  |  |
|  | A1 | Correct equation |  |  |
|  | DM1 | Dependent on second M1 (allow if $g$ missing) |  |  |
|  | A1 | Cao ( $R=215.2$ if they use $g=9.81$ ) |  |  |


| Question | Scheme | Marks | AOs |
| :---: | :---: | :---: | :---: |
| 2(a) | $\begin{array}{cc} 2 u \rightarrow & \leftarrow u \\ \frac{9 m u}{2} \longleftarrow \sim & \begin{array}{c}  \\ \\ v \leftarrow \end{array} \\ \rightarrow w \end{array} \longrightarrow \frac{9 m u}{2}$ |  |  |
|  | Use of Impulse-momentum principle for $A$ or $B$ | M1 | 3.4 |
|  | A: $\frac{9 m u}{2}=m(v--2 u) \quad$ or $\quad B: \frac{9 m u}{2}=3 m(w--u)$ | A1 | 1.1b |
|  | Use of Impulse-momentum principle for $B$ or $A$ or CLM | M1 | 3.4 |
|  | $\begin{aligned} & \frac{9 m u}{2}=3 m(w--u) \quad \text { or } \quad \frac{9 m u}{2}=m(v--2 u) \quad \text { or } \\ & 2 m u-3 m u=-m v+3 m w \end{aligned}$ | A1 | 1.1b |
|  | $v=\frac{5 u}{2}$ and $w=\frac{u}{2}$ | A1 | 1.1b |
|  | $e=\frac{\frac{5 u}{2}+\frac{u}{2}}{2 u+u}$ | M1 | 3.1a |
|  | $e=1$ | A1cso | 1.1b |
|  | ALTERNATIVE: |  |  |
|  | NEL is written down before $v$ and $w$ are found: $v+w=3 u e$ | $3^{\text {rd }}$ M1 |  |
|  | Use of Impulse-momentum principle for $A$ or $B$ | $1^{\text {st }} \mathrm{M} 1$ |  |
|  | $A: \quad \frac{9 m u}{2}=m(v--2 u) \quad$ or $\quad B: \frac{9 m u}{2}=3 m(w--u)$ | $1^{\text {st }} \mathrm{A} 1$ |  |
|  | Use of Impulse-momentum principle for B or $A$ or CLM | $2^{\text {nd }} \mathrm{M} 1$ |  |
|  | $\begin{aligned} & \frac{9 m u}{2}=3 m(w--u) \quad \text { or } \quad \frac{9 m u}{2}=m(v--2 u) \quad \text { or } \\ & 2 m u-3 m u=-m v+3 m w \end{aligned}$ | $2^{\text {nd }}$ A1 |  |
|  | An equation (not an identity) in $u$ and $e$ only is produced | $3{ }^{\text {rd }}$ A1 |  |
|  | $e=1$ | A1cso |  |
|  |  | (7) |  |
| 2(b) | Perfectly elastic (or the coefficient of restitution is 1 ) so no loss in kinetic energy. <br> Allow a direct evaluation of the KE loss i.e. $\frac{1}{2} m(2 u)^{2}+\frac{1}{2} \times 3 m u^{2}-\left(\frac{1}{2} m\left(\frac{5 u}{2}\right)^{2}+\frac{1}{2} \times 3 m\left(\frac{u}{2}\right)^{2}\right)=0$ <br> B0 if incorrect extras | DB1 | 2.4 |
|  |  | (1) |  |
| (8 marks) |  |  |  |

## Notes:

N.B. Ignore diagrams if it helps the candidate.

Equations need to be consistent, where appropriate, to earn A marks.

| 2a | M1 | Use of Impulse-momentum principle for $A$ or $B$, condone sign errors but M0 if dimensionally incorrect e.g. if $m$ missing |
| :---: | :---: | :---: |
|  | A1 | Correct unsimplified equation |
|  | M1 | Use of Impulse-momentum principle for other particle or CLM, condone sign errors but M0 if dimensionally incorrect e.g. if $m$ missing from impulse For CLM, allow consistent missing $m$ 's or extra $g$ 's. |
|  | A1 | Correct unsimplified equation |
|  | A1 | Cao for both. Allow one or both negative if correct for their symbols. |
|  | M1 | Use of NEL to obtain $e=\ldots$, condone sign errors in numerator but must be terms in $u$ only AND must be $(2 u+u)$ in denominator. <br> M0 if inverted |
|  | A1 | cso |
| 2b | DB1 | Dependent on $e=1$ correctly obtained in (a) <br> A correct statement e.g. zero, 0 etc and a correct reason |


| Question Scheme |  | Marks | AOs |
| :---: | :---: | :---: | :---: |
| 3(a) | $m g \times \frac{25}{6} \sin \alpha$ | B1 | 1.1b |
|  | Use of the principle of conservation of mechanical energy | M1 | 3.4 |
|  | $\frac{1}{2} m \times 25^{2}-\frac{1}{2} m v^{2}=m g \times \frac{25}{6} \sin \alpha$ | A1 | 1.1b |
|  | $v=24\left(\mathrm{~ms}^{-1}\right) \quad(23.99895831 \ldots=24$ to 2SF if $g=9.81)$ | A1 | 1.1b |
|  |  | (4) |  |
| 3(b) | Resolve perpendicular to the plane | M1 | 3.1a |
|  | $R=m g \cos \alpha$ | A1 | 1.1b |
|  | $F=\frac{3}{5} R$ | B1 | 3.4 |
|  | WD against friction $=F \times \frac{25}{6}$ | B1 | 3.4 |
|  | Use of work-energy principle | M1 | 3.1a |
|  | $\frac{1}{2} m \times 25^{2}-\frac{1}{2} m v^{2}=m g \times \frac{25}{6} \sin \alpha+\frac{3}{5} \times m g \cos \alpha \times \frac{25}{6}$ | $\begin{aligned} & \text { A1 } \\ & \text { A1 } \end{aligned}$ | $\begin{aligned} & 1.1 \mathrm{~b} \\ & 1.1 \mathrm{~b} \end{aligned}$ |
|  | $v=23.2 \text { or } 23\left(\mathrm{~ms}^{-1}\right)$ <br> (23.16700 $\ldots=23.2$ or 23 to 3SF or 2SF if $g=9.81$ ) | A1 | 1.1b |
|  |  | (8) |  |

(12 marks)

## Notes:

|  |  | N.B. If consistent use of a specific value of $m$, allow all the marks but deduct the final <br> A mark in each part but allow full marks if $m$ 's have been cancelled or don't appear. |
| :--- | :--- | :--- |
| 3a | B1 | Seen anywhere |
|  | M1 | Correct no. of terms, dimensionally correct, condone sign errors and sin/cos confusion <br> M0 for non-energy methods. <br> Allow max M1A0A0 if 25/6 not resolved or not resolved correctly in PE term |
|  | A1 | Correct equation in $m, g, v$ and $\alpha$ |$|$|  | A1 | cao |
| :--- | :---: | :--- |
| 3b | M1 | Correct no. of terms, dimensionally correct, condone sign errors and sin/cos confusion |
|  | A1 | Correct equation |
|  | B1 | Seen anywhere |
|  | B1 | Seen anywhere | | Correct no. of terms, dimensionally correct, condone sign errors and sin/cos confusion |
| :--- |
| M0 for non work-energy methods |
| Allow max M1A1A0A0 if 25/6 not resolved or not resolved correctly in PE term |


|  | A1 | Equation in $m, g, v$ and $\alpha$ with at most one error <br> N.B. If KE terms reversed, only penalise ONCE. |
| :--- | :--- | :--- |
|  | A1 | Correct equation in $m, g, v$ and $\alpha$ |
|  | A1 | cao |


| Question | Scheme | Marks | AOs |
| :---: | :---: | :---: | :---: |
| 4(a) | $2 u \rightarrow$ 0 <br> $P(2 m)$ $Q(3 m)$ <br> $w \leftarrow$ $\rightarrow v$ |  |  |
|  | Use of CLM | M1 | 3.4 |
|  | $2 m \times 2 u=-2 m w+3 m v$ | A1 | 1.1b |
|  | Use of NEL | M1 | 3.4 |
|  | $2 u e=w+v$ | A1 | 1.1b |
|  | Solve for $v$ | D M1 | 1.1b |
|  | $v=\frac{4 u(1+e)}{5} *$ | A1* | 2.2a |
|  |  | (6) |  |
| 4(b) | Since $0 \leq e \leq 1, \frac{4 u(1+0)}{5} \leq v \leq \frac{4 u(1+1)}{5}$ | M1 | 3.1a |
|  | i.e. $\frac{4 u}{5} \leq v \leq \frac{8 u}{5} *$ | A1* | 2.2a |
|  |  | (2) |  |
| 4(c) | Solve for $w$ | M1 | 1.1b |
|  | $w=\frac{2 u(3 e-2)}{5}$ oe ( $\mathrm{ms}^{-1}$ ) $\quad$ or $\left\|\frac{2 u(2-3 e)}{5}\right\|$ oe | A1 | 1.1b |
|  |  | (2) |  |
| 4(d) | Speed of $Q$ after hitting the wall $=\frac{1}{6} v \quad\left(\mathrm{~ms}^{-1}\right)$ | M1 | 3.4 |
|  | For a further collision between $P$ and $Q, \frac{1}{6} v>w$ | M1 | 3.1a |
|  | Substitute for $v$ and $w$ and solve for $e$ | M1 | 1.1b |
|  | $e<\frac{7}{8}$ | A1 | 1.1b |
|  | $\frac{2}{3}<e<\frac{7}{8}$ | A1 | 1.1b |
|  |  | (5) |  |
| (15 marks) |  |  |  |

## Notes:

| 4a | M1 | Correct no. of terms, condone sign errors, allow consistently cancelled $m$ 's or extra $g$ 's <br> or common factors throughout |
| :---: | :--- | :--- |
|  | A1 | Correct equation; they may have $w$ instead of $-w$ |
|  | M1 | Correct no. of terms, condone sign errors. M0 if $e$ on the wrong side of the equation |


|  | A1 | Correct equation; they may have $w$ instead of $-w$ |
| :---: | :---: | :---: |
|  | $\begin{aligned} & \mathrm{DM} \\ & 1 \end{aligned}$ | Solve for $v$, dependent on previous two marks |
|  | A1* | Correct answer correctly obtained |
| 4b | M1 | Use of $0 \leq e \leq 1$ in the given answer; allow use of $e=0$ and $e=1$ to obtain the min and max expressions <br> M1A0 for 'verification'. |
|  | A1* | Correct answer correctly obtained (including use of max and min) |
| 4c | M1 | Solve for their $w$ |
|  | A1 | cao |
| 4d | M1 | Speed so must see a positive quantity M0 if $\frac{1}{6}$ is on the wrong side of the equation |
|  | M1 | Correct inequality for their $w$ (allow even if their $w$ is dimensionally incorrect) |
|  | M1 | Independent M mark but must have an inequality in $v$ and $w$ : Substitute for $v$, using given answer, and $w$ and solve for $e$ |
|  | A1 | Correct upper bound for $e$ |
|  | A1 | cao |

